



Louisiana Important Prerequisite Math Standards

Now, more than ever, all students deserve access to engaging, challenging, grade-level math instruction. This is especially true for students who have been underserved such as students living in poverty, students from racially marginalized communities, students with learning differences, and students who are multilingual emergent. A commitment to <u>equitable instruction</u> requires that educators are intentional in identifying, celebrating, and building on knowledge that students have gained. It also requires that educators are strategic as they plan to address current and ongoing learning gaps. Starting the school year with weeks of review of prior-grade standards will result in a long-term loss of access to grade-level work that <u>perpetuates inequities¹</u> for historically marginalized students. This resource demonstrates that **students who were impacted by interruptions to teaching and learning and subsequent learning losses are still able to access most grade-level standards this year without prior review, and that missed content can usually be integrated in a minimally-invasive way. The Louisiana Department of Education has adapted this document, created by Achievement Network (Anet), to support the Louisiana Student Standards for Mathematics and implementation of Tier 1 Louisiana curricula.**

- What are the standards in this document? This document highlights important prerequisites to the Louisiana Student Standards for Mathematics in Grade 1 through Algebra I, as defined by ANet and informed by the <u>Coherence Map</u>, high-quality instructional materials, and review by Student Achievement Partners. It is meant to support the Understand, Diagnose, Take Action approach to address unfinished learning, as described <u>here</u>. As Geometry and Algebra II are less affected by learning loss in the prior year, they are not included here.
- How can these standards be used in planning for 2020-21 instruction? Teachers can use this document to identify which standards in their grade have critical prerequisites from the prior grade level that may interfere with a student's ability to access grade-level content. In combination with a diagnosis of student needs through reflection on LEAP 360 Diagnostic item performance as listed in the Diagnostic Mapping Documents, the Eureka Acceleration Tools, or other high quality data sources, teachers can use this information to adjust long-range plans in anticipation of when more time will be needed to support students. This aligns with NCTM's push (pp. 3, 7-8) to determine necessary prior knowledge and "provide just-in-time interventions during the school day that do not replace daily, grade-level instruction and are designed on the basis of the results from effective formative assessments." Finally, suggestions are included for when to preserve or reduce instructional time in order to create space for instructional recovery to take place. In addition to the suggestions, lesson level alignment to the most widely used Tier 1 Louisiana curricula has been added to flag planning and action points during the year for teachers. Before completely removing lessons or content, teachers should consider several factors including pacing, time of year, and anticipated learning gaps.

- Is this document meant to be used beyond the 2020-21 school year? While the categorization of prerequisites will remain relevant, the suggestions about instructional time particularly those that call for certain standards to be deprioritized should be considered unique to the current circumstances.
- What should we make of standards that have an important prerequisite that needs to be addressed and a recommended reduction in instructional time? These considerations should be weighed together, along with the needs of your group of students. For example, the time spent on a standard might be reduced from five days to three days by de-emphasizing one part of the standard, but prior-grade needs might be addressed within the first lesson through strategic choice of tasks.
- How does this information align with assessable content for LEAP 2025 summative tests? This document is designed to help teachers use time effectively by strategically prioritizing content during this unprecedented time and should be used in conjunction with LEAP 2025 assessment guidance to make instructional decisions. Please refer to the <u>Assessment Guidance Library</u> for grade-specific information about test design for LEAP 2025 assessments.

| Term | Meaning | Example | Actions to take |
|--------------------|--|---|--|
| "The bridge is up" | Address before grade-level instruction. Without this prior knowledge, students most likely do not have a way to access the grade-level standard. | A 7th-grader who has not learned how to divide positive fractions (6.NS.A.1) needs to build that understanding before beginning to divide negative fractions (7.NS.A.2c). | Students may require dedicated instruction on prerequisite standards before the grade level instruction is taught. (Not every standard needs its own full lesson; multiple standards may be addressed at once, or a standard might be taught as a short mini-lesson.) |
| "Heavy traffic" | Address within grade-level instruction. Students will have an entry point into grade-level content, but will benefit from instruction that weaves in this prior-grade content. | A 4th-grader who struggles with recalling multiplication facts (3.OA.C.7) can still access grade-level, multi-step application problems (4.OA.A.3) when given a multiplication table, but will need small doses of continued support to attain fluency. | Individual tasks or strategies from these standards can be incorporated into grade-level lessons to address important content that was missed in the prior grade. |

Important Prerequisite Math Standards by Grade

| <u>Grade 1</u> 3 | <u>Grade 4</u> 17 | <u>Grade 7</u> 37 |
|-------------------|-------------------|---------------------|
| <u>Grade 2</u> 7 | <u>Grade 5</u> 23 | <u>Grade 8</u> 45 |
| <u>Grade 3</u> 11 | <u>Grade 6</u> 30 | <u>Algebra I</u> 51 |



Grade 1 Math Important Prerequisites

K-1 note: There is a significant degree of overlap between kindergarten and 1st grade standards. High-quality instructional materials embrace this overlap and provide teachers with resources to meet students where they are. For this reason, when kindergarten standards are listed as "heavy traffic" below, this should be interpreted as an area where emphasis is needed on certain problems and/or strategies; additional tasks may not need to be added. For example, word problems within 10 (K.OA.A.2) are likely already addressed within 1st grade curricular materials before problems within 20 (1.OA.A.1).

| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP quidance</u> | Comments related to most widely used Tier 1 Curriculum Eureka Math |
|---|--|---|--|---|
| K.OA.A.2 | ■1.OA.A.1 Application | Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. | Emphasize problems that involve sums less than or equal to 10 and/or the related differences to keep the focus on making sense of different problem types; do not limit the range of addition and subtraction situations, but assign fewer problems with sums greater than 10 or related differences. | |
| | ■1.OA.A.2 Application | Solve word problems that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem. | Reduce the amount of time spent on lessons and problems that call for addition of three whole numbers. Limit the amount of required student practice. | 2.1. |
| | ■1.OA.B.3 Conceptual | Apply properties of operations to add and subtract. <i>Examples: If</i> $8 + 3 = 11$ <i>is known, then</i> $3 + 8 = 11$ <i>is also known. (Commutative property of addition.) To add</i> $2 + 6 + 4$, <i>the second two numbers can be added to make a ten, so</i> $2 + 6 + 4 = 2 + 10 = 12$. (Associative property of addition.) | | |
| | ■1.OA.B.4 Conceptual | Understand subtraction as an unknown-addend problem. For example, subtract 10 - 8 by finding the number that makes 10 when added to 8. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|----------------------------------|---|---|--|--|
| | ■ 1.OA.C.5 Conceptual | Relate counting to addition and subtraction (e.g., by counting on 2 to add 2). | Integrate counting into the work of the domain (OA), instead of separate lessons, in order to reduce the amount of time spent on this standard. | 1.3, 1.6, 1.7, 1.26, 1.27, 2.5, 2.9, 2.12, 2.13, 2.14, 2.15, 2.16, 2.17, 2.19 (R), 2.21 (E) |
| K.OA.A.3 K.OA.A.4 K.OA.A.5 | | Add and subtract within 20, demonstrating fluency for addition and subtraction within 10. Use strategies such as counting on; making ten (e.g., $8 + 6 = 8 + 2 + 4 = 10 + 4 = 14$); decomposing a number leading to a ten (e.g., $13 - 4 = 13 - 3 - 1 = 10 - 1 = 9$); using the relationship between addition and subtraction (e.g., knowing that $8 + 4 = 12$, one knows $12 - 8 = 4$); and creating equivalent but easier or known sums (e.g., adding $6 + 7$ by creating the known equivalent $6 + 6 + 1 = 12 + 1 = 13$). | | |
| | , | Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false. For example, which of the following equations are true and which are false? $6 = 6$, $7 = 8 - 1$, $5 + 2 = 2 + 5$, $4 + 1 = 5 + 2$. | | |
| | Concentual | Determine the unknown whole number in an addition or subtraction equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 + ? = 11$, $5 = -3$, $6 + 6 =$ | | |
| | ■ 1.NBT.A.1 Conceptual Procedural | Count to 120, starting at any number less than 120. In this range, read and write numerals and represent a number of objects with a written numeral. | Eliminate lessons that are solely about extending the count sequence in order to reduce the amount of time spent on this cluster. Incorporate extending the count sequence into other lessons in the grade. | 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.11, 4.12, 6.3, 6.4, 6.7, 6.9 |
| | ■ 1.NBT.B.2 Conceptual | Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: | | |
| | ■ 1.NBT.B.2a Conceptual | 10 can be thought of as a bundle of ten ones — called a "ten." | | |
| K.NBT.A.1 | ■ 1.NBT.B.2b Conceptual | The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones. | | |
| | 1.NBT.B.2c Conceptual | The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones). | | |



| Prerequisite | Grade-Level | Standard Language | Instructional Time | Eureka Math |
|--------------|--------------------------|---|---|------------------------|
| Standard | Standard | | | |
| K.CC.C.7 | ■1.NBT.B.3 | Compare two two-digit numbers based on meanings of the tens and ones digits, recording the | | |
| | Conceptual | results of comparisons with the symbols >, =, and <. | | |
| | | Add within 100, including adding a two-digit number and a one-digit number, and adding a two- | | |
| | | digit number and a multiple of 10. | | |
| | ■1.NBT.C.4 | a. Use concrete models or drawings and strategies based on place value, properties of | | |
| | Conceptual | operations, and/or the relationship between addition and subtraction; relate the strategy | | |
| | Procedural | to a number sentence; justify the reasoning used with a written explanation. | | |
| | | b. Understand that in adding two-digit numbers, one adds tens and tens, ones and ones; and | | |
| | | sometimes it is necessary to compose a ten. | | |
| | ■1.NBT.C.5 | Given a two-digit number, mentally find 10 more or 10 less than the number, without having to | | |
| | Conceptual | count; explain the reasoning used. | | |
| | | Subtract multiples of 10 in the range 10-90 from multiples of 10 in the range 10-90 (positive or | | |
| | ■1.NBT.C.6 | zero differences), using concrete models or drawings and strategies based on place value, | | |
| | Conceptual | properties of operations, and/or the relationship between addition and subtraction; relate the | | |
| | | strategy to a written method and explain the reasoning used. | | |
| | ■1.MD.A.1 | Order three objects by length; compare the lengths of two objects indirectly by using a third | | |
| | Conceptual Procedural | object. | | |
| | | Express the length of an object as a whole number of length units, by laying multiple copies of a | | |
| | ■1.MD.A.2 | shorter object (the length unit) end to end; understand that the length measurement of an object | | |
| | Conceptual | is the number of same-size length units that span it with no gaps or overlaps. Limit to contexts | | |
| | Procedural | where the object being measured is spanned by a whole number of length units with no gaps or | | |
| | | overlaps. | | |
| | 01.MD.B.3 | | Eliminate lessons devoted to | |
| | Conceptual Procedural | Tell and write time in hours and half-hours using analog and digital clocks. | telling and writing time to the hour and half-hour. | 5.10, 5.11, 5.12, 5.13 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|---|---|---|
| Standard | ■1.MD.C.4 Conceptual Procedural Application | Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another. | Eliminate lessons devoted to representing and interpreting data. (Do not eliminate problems about using addition and subtraction to solve problems about the data.) | 3.10, 3.11 (E), 3.12, 3.13 |
| | □1.MD.D.5 Procedural | Determine the value of a collection of coins up to 50 cents. (Pennies, nickels, dimes, and quarters in isolation; not to include a combination of different coins.) | Eliminate lessons devoted to valuing a set of coins. | This standard is not addressed in Eureka Math. |
| K.G.A.2 K.G.B.4 | ○1.G.A.1 Conceptual | Distinguish between defining attributes (e.g., triangles are closed and three-sided) versus non- defining attributes (e.g., color, orientation, overall size); build and draw shapes to possess defining attributes. | Combine lessons to address key concepts of defining attributes of shapes and composing shapes in order to reduce the amount of time spent on this cluster. | 5.4, 5.5, 5.6 |
| | ●1.G.A.2 Conceptual | Compose two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) and three-dimensional shapes (cubes, right rectangular prisms*, right circular cones, and right circular cylinders) to create a composite shape, and compose new shapes from the composite shape. *Students do not need to learn formal names such as "right rectangular prism." | | |
| | ○1.G.A.3 Conceptual Procedural | Partition circles and rectangles into two and four equal shares, describe the shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. Describe the whole as two of, or four of the shares. Understand for these examples that decomposing into more equal shares creates smaller shares. | | |



Grade 2 Math Important Prerequisites

| Prerequisite Standard | Grade-Level Standard | | Instructional Time | Comments related to most widely |
|--|---|--|---|--|
| Bridge up or heavy traffic from previous grade | Major Supporting Additional | Standard Language | 20-21 as compared to a typical year, per <u>SAP quidance</u> | used Tier 1 Curriculum Eureka Math |
| 1.0A.A.1 1.0A.D.8 | ■2.OA.A.1 Application | Use addition and subtraction within 100 to solve one- and two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem. | Emphasize problems that involve sums less than or equal to 20 and/or the related differences to keep the focus on making sense of different problem types; assign fewer problems with sums greater than 20 or related differences. | |
| 1.OA.C.6 | ■2.OA.B.2 Procedural | Fluently add and subtract within 20 using mental strategies. By end of Grade 2, know from memory all sums of two one-digit numbers. | Incorporate additional practice on the grade 1 fluency of adding and subtracting within 10 (1.OA.C.6) early in the school year to support the addition and subtraction work of grade 2 (2.OA). | |
| | 2.OA.C.3 Conceptual | Determine whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; write an equation to express an even number as a sum of two equal addends. | Eliminate lessons on foundations for | 6.17, 6.18, 6.19 |
| | 2.OA.C.4 Conceptual | Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends. | multiplication. | 6.6, 6.7, 6.8, 6.9, 6.10, 6.11, 6.12, 6.13, 6.14, 6.15 |
| 1.NBT.B.2a-c | 2.NBT.A.1 Conceptual | Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. | | |
| | 2.NBT.A.1a Conceptual | 100 can be thought of as a bundle of ten tens called a hundred. | | |
| 1.NBT.B.2a-c | 2.NBT.A.1b Conceptual | The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones). | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|--|--|--|
| | 2.NBT.A.2 Procedural | Count within 1000; skip-count by 5s, 10s, and 100s. | Integrate lessons and practice on these standards into the | 3.2, 3.3, 3.4, 3.8, 3.9, 3.12, 3.13, 3.14, 3.15 (E), 3.19, 3.20, 3.21 (E), 7.21, 8.14 |
| | ■2.NBT.A.3 Conceptual Procedural | Read and write numbers to 1000 using base-ten numerals, number names, and expanded form. | work of place value. Limit the amount of required student practice on counting by ones, reading/writing, and comparing numbers. | 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9, 3.14, 3.16, 3.17, 3.18 (E) |
| 1.NBT.B.3 | 2.NBT.A.4 Conceptual | Compare two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using >, =, and < symbols to record the results of comparisons. | | 3.16, 3.17, 3.18 (E) |
| 1.NBT.C.5, 1.NBT.C.6 | 2.NBT.B.5 Procedural | Fluently add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction. | Prioritize strategies based on place value in written work to strengthen the progression toward fluency with multi- digit addition and subtraction. | |
| | 2.NBT.B.6 Conceptual, Procedural | Add up to four two-digit numbers using strategies based on place value and properties of operations. | | |
| 1.OA.A.2 | ■ 2.NBT.B.7 Conceptual, Procedural | Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; justify the reasoning used with a written explanation. Understand that in adding or subtracting three-digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds. | | |
| | 2.NBT.B.8 Conceptual | Mentally add 10 or 100 to a given number 100 to 900, and mentally subtract 10 or 100 from a given number 100 to 900. | | |
| | 2.NBT.B.9 Conceptual | Explain why addition and subtraction strategies work, using place value and the properties of operations. Explanations may be supported by drawings or objects. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|---------------------------------------|--|---|------------------------------------|
| 1.MD.A.2 | 2.MD.A.1 Procedural | Measure the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes. | | 2.4, 2.5, 2.9, 7.15, 7.16, 7.17 |
| | 2.MD.A.2 Conceptual, Procedural | Measure the length of an object twice, using length units of different lengths for the two measurements; describe how the two measurements relate to the size of the unit chosen. | Integrate lessons and practice into the work of measuring length with tools (2.MD.A.1) | 2.7, 7.18 |
| | ■2.MD.A.3 Conceptual | Estimate lengths using units of inches, feet, centimeters, and meters. | in order to reduce the amount of time spent on this cluster. Limit the amount of required | 2.5, 2.9, 7.17 |
| | ■2.MD.A.4 Procedural | Measure to determine how much longer one object is than another, expressing the length difference in terms of a standard unit length. | student practice. | 2.3, 2.6, 2.7, 2.9, 7.15, 7.19 |
| | 2.MD.B.5 Application | Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem. | Ensure word problems represent all grade 2 problem types, and refer to guidance for 2.OA.A. | |
| | 2.MD.B.6 Conceptual | Represent whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the number 0, 1, 2,, and represent whole-number sums and differences within 100 on a number line diagram. | | |
| 1.MD.B.3 | 2.MD.C.7 Conceptual, Procedural | Tell and write time from analog and digital clocks to the nearest five minutes, using a.m. and p.m. | Combine lessons in order to reduce the amount of time spent. Emphasize denominations that support | 8.13, 8.14, 8.15 |
| | 2.MD.C.8 Application | Solve word problems involving dollar bills, quarters, dimes, nickels, and pennies, using \$ and ¢ symbols appropriately. <i>Example: If you have 2 dimes and 3 pennies, how many cents do you have?</i> | place value understanding such as penny-dime- dollar. Limit the amount of required student practice. | 3.10, 7.6, 7.7, 7.8, 7.12, 7.13 |
| | 2.MD.D.9 Procedural | Generate measurement data by measuring lengths of several objects to the nearest whole unit, or by making repeated measurements of the same object. Show the measurements by making a line plot, where the horizontal scale is marked off in whole-number units. | Eliminate lessons on these standards. Integrate data displays only | 7.23, 7.24, 7.25, 7.26(R) |
| | 2.MD.D.10 Procedural | Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. Solve simple put-together, take-apart, and compare problems using information presented in a bar graph. | as settings for addition & subtraction word problems (2.OA.A). | 7.1, 7.2, 7.3, 7.4, 7.5 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--------------------------------------|---|--|--|
| | 2.G.A.1 Conceptual, Procedural | Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. Identify triangles, quadrilaterals, pentagons, hexagons, and cubes. | Combine lessons to address | 8.2, 8.3, 8.4, 8.5, 8.6 |
| | 2.G.A.2 Conceptual, Procedural | number of them. | the amount of time spent on this cluster. Limit the amount of required student practice. | 6.14, 6.15 |
| 1.G.A.3 | 2.G.A.3 Conceptual, Procedural | Dartition circles and restangles into two three, or four equal shares, describe the shares using the | | 8.7, 8.8, 8.9, 8.10, 8.11, 8.12, 8.13 |



| | Grade 3 Math Important Prerequisites | | | | |
|---|--|---|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP guidance</u> | Comments related to most widely used Tier 1 Curriculum Eureka Math | |
| | ■3.OA.A.1 Conceptual | Interpret products of whole numbers, e.g., interpret 5 × 7 as the total number of objects in 5 groups of 7 objects each. <i>For example, describe a context in which a total number of objects can be expressed as 5</i> × 7. | | | |
| 2.NBT.A.2, 2.OA.C.3, | ■3.OA.A.2 Conceptual | Interpret whole-number quotients of whole numbers, e.g., interpret 56 \div 8 as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. For example, describe a context in which a number of shares or a number of groups can be expressed as 56 \div 8. | Students may need extra support to see row and | | |
| 2.0A.C.4 | ■3.OA.A.3 Application | Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem. *Table 2 can be found in the Louisiana Student Standards for Mathematics | column structure in arrays of objects. | | |
| | ■3.OA.A.4 Conceptual | Determine the unknown whole number in a multiplication or division equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = _ \div 3$, $6 \times 6 = ?$. | - | | |
| 2.NBT.B.5 | ■3.OA.B.5 Conceptual | Apply properties* of operations as strategies to multiply and divide. (Students need not use formal terms for these properties.) <i>Examples: If</i> $6 \times 4 = 24$ <i>is known, then</i> $4 \times 6 = 24$ <i>is also known.</i> (<i>Commutative property of multiplication.</i>) $3 \times 5 \times 2$ <i>can be found by</i> $3 \times 5 = 15$ <i>then</i> $15 \times 2 = 30$, <i>or by</i> $5 \times 2 = 10$ <i>then</i> $3 \times 10 = 30$. (<i>Associative property of multiplication.</i>) <i>Knowing that</i> $8 \times 5 = 40$ <i>and</i> $8 \times 2 = 16$, <i>one can find</i> 8×7 <i>as</i> $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (<i>Distributive property of multiplication.</i>) *Students need not use formal terms for these properties. | | | |
| | ■3.OA.B.6 Conceptual | Understand division as an unknown-factor problem. <i>For example, find 32 ÷ 8 by finding the number that makes 32 when multiplied by 8.</i> | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--|---|--|--|---------------------------------------|
| | ■3.OA.C.7 Procedural | Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers. | | |
| 2.0A.A.1 | ■ 3.0A.D.8 Conceptual Application | Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. *This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in the conventional order when there are no parentheses to specify a particular order. | | |
| | ■3.OA.D.9 Conceptual | Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends. | Eliminate lessons or problems on arithmetic patterns. | 3.1, 3.13, 3.14, 3.16, 3.17, 3.19 |
| | • 3.NBT.A.1 Conceptual | Use place value understanding to round whole numbers to the nearest 10 or 100. | Combine lessons on rounding in order to reduce the amount of time spent on rounding numbers. Limit the amount of required student practice. | 2.12, 2.13, 2.14, 2.17, 2.20, 2.21 |
| 2.NBT.A.1, 2.NBT.B.7, 2.NBT.B.8, 2.NBT.B.9, 2.OA.B.2 | •3.NBT.A.2 Procedural | Fluently add and subtract within 1000 using strategies and algorithms* based on place value, properties of operations, and/or the relationship between addition and subtraction. * A range of algorithms may be used. | | |
| | •3.NBT.A.3 Conceptual, Procedural | Multiply one-digit whole numbers by multiples of 10 in the range 10-90 (e.g., 9 × 80, 5 × 60) using strategies based on place value and properties of operations. | Combine lessons in order to reduce time spent multiplying by multiples of 10. Emphasize the connection to single-digit products and tens units. | 3.19, 3.20 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--------------------------|--|---|-------------|
| 2.MD.A.2, 2.G.A.3 | ■3.NF.A.1 Conceptual | Understand a fraction 1/b, with denominators 2, 3, 4, 6, and 8, as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size 1/b. | | |
| | ■3.NF.A.2 Conceptual | Understand a fraction with denominators 2, 3, 4, 6, and 8 as a number on the number line diagram. | | |
| 2.MD.B.6 | ■3.NF.A.2a Conceptual | Represent a fraction 1/b on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size 1/b and that the endpoint of the part based at 0 locates the number 1/b on the number line. | | |
| | ■3.NF.A.2b Conceptual | Represent a fraction a/b on a number line diagram by marking off a lengths 1/b from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line. | Emphasize the concept of unit fraction as the basis for building fractions. Prioritize the number line | |
| | ■3.NF.A.3 Conceptual | Explain equivalence of fractions with denominators 2, 3, 4, 6, 8 in special cases, and compare fractions by reasoning about their size. | as a representation to develop students' understanding of fractions | |
| | ■3.NF.A.3a Conceptual | Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line. | as numbers by foregrounding the magnitude, location, and order of fractions among | |
| | ■3.NF.A.3b Conceptual | Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. Explain why the fractions are equivalent, e.g., by using a visual fraction model. | whole numbers (3.NF.A.2) | |
| | ■3.NF.A.3c Conceptual | Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a number line diagram. | | |
| | Conceptual | Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|---|---|---|
| | ■3.MD.A.1 Conceptual | Understand time to the nearest minute. | | see alignment for 3.MD.A.1a and 3.MD.A.1c |
| 2.MD.C.7 | ■3.MD.A.1a Conceptual, Procedural | Tell and write time to the nearest minute and measure time intervals in minutes, within 60 minutes, on an analog and digital clock. | | 2.3 |
| 2.1010.0.7 | ■3.MD.A.1b Procedural | Calculate elapsed time greater than 60 minutes to the nearest quarter and half hour on a number line diagram. | Combine lessons in order to reduce the amount of time spent on time, volume, and mass. Reduce the amount of required student practice. | Eureka math contains no direct alignment to this part of 3.MD.A.1 |
| | ■3.MD.A.1c Application | Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram. | | 2.4, 2.5, 2.15, 2.16, 2.17, 2.18, 2.21 |
| | ■3.MD.A.2 Conceptual, Procedural, Application | Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (I). Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem. * Excludes compound units such as cm3 and finding the geometric volume of a container. ** Excludes multiplicative comparison problems (problems involving notions of "times as much"). | | 2.6, 2.7, 2.8, 2.9. 2.10, 2.11, 2.12, 2.15, 2.16, 2.17, 2.18, 2.19, 2.20, 2.21 |
| | 3.MD.B.3 Procedural, Application | Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs. For example, draw a bar graph in which each square in the bar graph might represent 5 pets. | Eliminate lessons on creating scaled graphs. Integrate a few problems with scaled graphs only as settings for multiplication word problems (3.OA.A.3) and two-step word problems (3.OA.D.8). | 6.1, 6.2, 6.3, 6.4, 6.9 |
| | 3.MD.B.4 Conceptual, Procedural | Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units - whole numbers, halves, or quarters. | Eliminate any lessons or problems that do not strongly reinforce the fraction work of this grade (3.NF.A). | 6.5, 6.6, 6.7, 6.8, 6.9 7.19, 7.22, 7.26 (E) |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|---|--|---|---|
| 2.MD.A.1 | ■3.MD.C.5 Conceptual | Recognize area as an attribute of plane figures and understand concepts of area measurement. | | 4.1, 4.2, 4.3, 4.4 |
| | ■3.MD.C.5a Conceptual | A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used to measure area. | Emphasize enduring concepts of geometric | 4.1, 4.2, 4.3, 4.4 |
| | ■3.MD.C.5b Conceptual | A plane figure which can be covered without gaps or overlaps by <i>n</i> unit squares is said to have an area of <i>n</i> square units. | | 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.13 (E) |
| 2.G.A.2 | ■3.MD.C.6 Procedural | Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units). | J-p | 4.1, 4.2, 4.3, 4.4, 4.5, 4.6, 4.7, 4.13 (E) |
| | ■3.MD.C.7 Conceptual | Relate area to the operations of multiplication and addition. | students using area models to support their mathematical explanations involving the | 4.4, 4.5, 4.6, 4.7, 4.8, 4.9, 4.10, 4.11 |
| | ■3.MD.C.7a Conceptual. Procedural | Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths. | distributive property for products (3.MD.C.7c). Combine lessons in order to reduce the amount of | 4.4, 4.5, 4.6, 4.7, 4.8 |
| | ■3.MD.C.7b Conceptual, Procedural, Application | Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning. | time spent on measuring area and limit the amount of required student | 4.5, 4.6, 4.7, 4.8, 4.9, 4.10, 4.11, 4.12, 4.13 (E), 4.14 (E), 4.15 (E), 4.16 (E) 7.28, 7.29, 7.30 |
| | ■3.MD.C.7c Conceptual | Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and b + c is the sum of a × b and a × c. Use area models to represent the distributive property in mathematical reasoning. | | 4.9, 4.10, 4.11, 4.12 |
| | •3.MD.D.8 Procedural, Application | Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters. | Integrate a few problems on perimeter into work on area (3.MD.C). | 7.12, 7.13, 7.14, 7.15, 7.17, 7.18, 7.19, 7.20, 7.21, 7.22, 7.23, 7.24 (E), 7.25 (E), 7.26 (E), 7.27 (E), 7.28, 7.29, 7.30 |
| | 3.MD.E.9 Application | Solve word problems involving pennies, nickels, dimes, quarters, and bills greater than one dollar, using the dollar and cent symbols appropriately. | Eliminate lessons solely used to address this standard. | Eureka math contains no direct alignment to this standard |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|---------------------------|--|--|--|
| 2.G.A.1 | Conceptual, Procedural | attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw | Combine lessons on shapes and their attributes in order to reduce the amount of time spent on this standard. | 7.4, 7.5 |
| 2.G.A.2 | - 5.0.A.Z | whole. For example, partition a shape into 4 parts with equal area, and describe the area of each part as | Eliminate separate geometry lessons on partitioning shapes | 5.3, 5.4, 5.5, 5.6, 5.7, 5.8, 5.9, 5.10, 5.11, 5.13 (R), 5.24, 5.25, 5.27 (R), 5.28, 5.29 |



Grade 4 Math Important Prerequisites

| | Grade 4 Math Important Prerequisites | | | | | | |
|---|--|---|--|--|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP quidance</u> | Comments related to most widely used Tier 1 Curriculum Eureka Math | | | |
| 3.OA.A.1, 3.OA.A.2, | ■4.OA.A.1 Conceptual | Interpret a multiplication equation as a comparison and represent verbal statements of multiplicative comparisons as multiplication equations, e.g., interpret 35 = 5 x 7 as a statement that 35 is 5 times as many as 7 and 7 times as many as 5. | | | | | |
| 3.0A.A.2, 3.0A.B.6, 3.0A.C.7 | 4.OA.A.2 Application | Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison. (Example: 6 times as many vs 6 more than.) *Table 2 found in the Louisiana Student Standards for Mathematics has been added to the end of this document. | | | | | |
| 3.0A.C.7, 3.0A.D.8 | ■4.OA.A.3 Conceptual Application | Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding. Example: Twenty-five people are going to the movies. Four people fit in each car. How many cars are needed to get all 25 people to the theater at the same time? | | | | | |
| | 4.OA.B.4 Conceptual, Procedural | Using whole numbers in the range 1–100 | | | | | |
| | 4.OA.B.4a Procedural | Find all factor pairs for a given whole number. | | | | | |
| | 4.OA.B.4b Conceptual | Recognize that a given whole number is a multiple of each of its factors | | | | | |
| | 4.OA.B.4c Conceptual | Determine whether a given whole number is a multiple of a given one-digit number. | | | | | |
| | 4.OA.B.4d Conceptual | Determine whether a given whole number is prime or composite. | | | | | |



| Prerequisite | Grade-Level | Standard Language | Instructional Time | Eureka Math |
|--|---|--|---|--|
| Standard 3.OA.D.9 | •4.0A.C.5 Conceptual, Procedural | Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. For example, given the rule "Add 3" and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way. | Eliminate lessons on | 5.41 |
| | ■4.NBT.A.1 | Recognize that in a multi-digit whole number less than or equal to 1,000,000, a digit in one place represents ten times what it represents in the place to its right. Examples: (1) recognize that $700 \div 70 =$ 10; (2) in the number 7,246, the 2 represents 200, but in the number 7,426 the 2 represents 20, recognizing that 200 is ten times as large as 20, by applying concepts of place value and division. | | |
| | , | Read and write multi-digit whole numbers less than or equal to 1,000,000 using base-ten numerals, number names, and expanded form. Compare two multi-digit numbers based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons. | | |
| 3.NBT.A.1 | ■4.NBT.A.3 Conceptual | Use place value understanding to round multi-digit whole numbers, less than or equal to 1,000,000, to any place. | First tasks should involve rounding to tens and hundreds. | |
| 3.NBT.A.2 | 4.NBT.B.4 Procedural | Fluently add and subtract multi-digit whole numbers with sums less than or equal to 1,000,000, using the standard algorithm | Emphasize problems with only one regrouping step. | 1.11, 1.12, 1.13, 1.14, 1.15, 1.16, 1.17, 1.18, 1.19 (E) 2.1, 2.2, 2.3, 2.5 |
| 3.MD.C.7a-c, 3.NBT.A.3, 3.OA.A.1, 3.OA.B.5, 3.OA.C.7 | Conceptual, | Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. | | |
| 3.0A.A.2, 3.0A.B.5, 3.0A.B.6, 3.0A.C.7 | ■4.NBT.B.6 Conceptual, Procedural | Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|----------------------------|--|--|---|-------------|
| 3.NF.A.1 | ■4.NF.A.1 Conceptual, Procedural | Explain why a fraction a/b is equivalent to a fraction ($n \ge a$)/($n \ge b$) by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.) | Incorporate some foundational work on the meaning of the unit | |
| 3.NF.A.2a-b 3.NF.A.3a-d | ■4.NF.A.2 Conceptual | Compare two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as 1/2. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with symbols >, =, or <, and justify the conclusions, e.g., by using a visual fraction model. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.) | fraction (3.NF.A.1 & 2), especially through partitioning the whole on a | |
| | ■4.NF.B.3 Conceptual | Understand a fraction <i>a/b</i> with <i>a</i> > 1 as a sum of fractions 1/ <i>b</i> . (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.) | Emphasize reasoning with unit fractions to determine sums and products, not committing calculation rules to memory or engaging in repetitive fluency exercises. | |
| | ■4.NF.B.3a Conceptual | Understand addition and subtraction of fractions as joining and separating parts referring to the same whole. Example: $3/4 = 1/4 + 1/4 + 1/4$. | | |
| | 4.NF.B.3b Conceptual | Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. Examples: $3/8 = 1/8 + 1/8 + 1/8$; $3/8 = 1/8 + 2/8$; $2 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$. | | |
| | ■4.NF.B.3c Procedural | Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction. | | |
| | ■4.NF.B.3d Application | Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem. | | |
| | ■4.NF.B.4 Procedural | Multiply a fraction by a whole number. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.) | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|---|---|--------------------|-------------|
| | ■4.NF.B.4a Conceptual | Understand a fraction a/b as a multiple of 1/b. For example, use a visual fraction model to represent 5/4 as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$. | | |
| | ■4.NF.B.4b Conceptual, Procedural | Understand a multiple of a/b as a multiple of 1/b, and use this understanding to multiply a fraction by a whole number. For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.) | | |
| | ■4.NF.B.4c Application | Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. <i>For example, if each person at a party will eat 3/8 of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole numbers does your answer lie?</i> | | |
| | ■4.NF.C.5 Conceptual, Procedural | Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. For example, express $3/10$ as $30/100$ and add $3/10 + 4/100 = 34/100$. (Students who can generate equivalent fractions can develop strategies for adding fractions with unlike denominators in general, but addition and subtraction with unlike denominators in general is not a requirement at this grade.) | | |
| | ■4.NF.C.6 Procedural | Use decimal notation for fractions with denominators 10 or 100. For example, rewrite 0.62 as 62/100; describe a length as 0.62 meters; locate 0.62 on a number line diagram; represent 62/100 of a dollar as \$0.62. | | |
| | ■4.NF.C.7 Conceptual | Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions, e.g., by using a visual model. | | |
| 3.MD.A.2 | 4.MD.A.1 Conceptual, Procedural | Know relative sizes of measurement units within one system of units including: ft, in; km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. (Conversions are limited to one-step conversions.) Record measurement equivalents in a two-column table. <i>For example: Know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36),</i> | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|--|--|--|
| | 4.MD.A.2 Conceptual, Application | Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving whole numbers and/or simple fractions (addition and subtraction of fractions with like denominators and multiplying a fraction times a fraction* or a whole number), and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale. * Students in Grade 4 will be assessed on multiplying a fraction and a whole number as indicated in the NF domain. Some students may be able to multiply a fraction by a fraction as a result of generating equivalent fractions; however, mastery of multiplying two fractions occurs in Grade 5. | Combine lessons on problems involving measurement, except for those on measurement conversion (see 4.MD.A.1). Limit the amount of required student practice. | 2.1, 2.2, 2.3, 2.5 5.40 6.14, 6.16 7.1, 7.2, 7.3, 7.4, 7.6, 7.7, 7.8, 7.9, 7.10, 7.11, 7.14 |
| 3.MD.D.8 | 4.MD.A.3 Application, Procedural | Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor. | | 3.1, 3.2, 3.3 7.15, 7.16 |
| | 4.MD.B.4 Procedural, Application | Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection. | Eliminate lessons and problems that do not strongly reinforce the fraction work of this grade (4.NF). | 5.28, 5.40 |
| | •4.MD.C.5 Conceptual | Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement: | - / · · · ·/ | 5.41 |
| | 4.MD.C.5a Conceptual 4.MD.C.5b Conceptual | An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle. An angle that turns through 1/360 of a circle is called a "one-degree angle," and can be used to measure angles. | Emphasize the foundational understanding of a one- degree angle as a unit of measure (4.MD.C.5a and b) and use that as the basis | |
| | •4.MD.C.5c Conceptual •4.MD.C.6 Procedural | An angle that turns through <i>n</i> one-degree angles is said to have an angle measure of <i>n</i> degrees. Measure angles in whole-number degrees using a protractor. Sketch angles of specified measure. | for measuring and drawing angles with protractors (4.MD.C.6). | 4.5, 4.6, 4.7, 4.8 |
| | •4.MD.C.7 Application, Procedural | Recognize angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in real world and mathematical problems, e.g., by using an equation with a symbol for the unknown angle measure. | Eliminate lessons on recognizing angle measure as additive. | 4.9, 4.10, 4.11 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|--|--|---|
| | •4.MD.D.8 Conceptual, Application, Procedural | rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real- | Eliminate lessons on recognizing area as additive. | 7.15, 7.16 |
| | •4.G.A.1 Conceptual, Procedural | Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in two-dimensional figures. | | 4.1, 4.2, 4.3, 4.4, 4.13, 4.14, 4.15 |
| | •4.G.A.2 Procedural | the presence or absence of angles of a specified size. Recognize right triangles as a category, and | properties. Limit the | 4.13, 4.14, 4.15 |
| | ○4.G.A.3 Conceptual, Procedural | Recognize a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. Identify line-symmetric figures and draw lines of symmetry. | amount of required student practice. | 4.12, 4.14 |



| | Grade 5 Math Important Prerequisites | | | | | | |
|--|--|---|--|--|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP quidance</u> | Comments related to most widely used Tier 1 Curriculum Eureka Math | | | |
| | •5.OA.A.1 Conceptual, Procedural | Use parentheses or brackets in numerical expressions, and evaluate expressions with these symbols | Combine lessons on writing and interpreting numerical expressions in order to reduce the amount of time | 2.1, 2.3, 2.4, 2.5 4.10, 4.32 | | | |
| | •5.0A.A.2 Conceptual | Write simple expressions that record calculations with whole numbers, fractions, and decimals, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as 2 × (8 + 7). Recognize that 3 × (18,932 + 9.21) is three times as large as 18,932 + 9.21, without having to calculate the indicated sum or product. | | 2.3, 2.4 4.10, 4.32 | | | |
| | ◦5.OA.B.3 Conceptual, Procedural | Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule "Add 3" and the starting number 0, and given the rule "Add 6" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so. | Eliminate lessons and | 6.7 | | | |



| Prerequisite | Grade-Level | Standard Language | Instructional Time | Eureka Math |
|--|--|--|---|-------------|
| Standard | Standard | | | |
| 4.NBT.A.1, 4.NF.C.5, 4.NF.C.6, 4.NF.C.7 | ■5.NBT.A.1 Conceptual | Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left. | | |
| | ■5.NBT.A.2 Conceptual, Procedural | Explain and apply patterns in the number of zeros of the product when multiplying a number by powers of 10. Explain and apply patterns in the values of the digits in the product or the quotient, when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10. For example, $10^0 = 1$, $10^1 = 10$ and $2.1 \times 10^2 = 210$. | Allow for time to develop students' understanding on foundation work of decimal | |
| | ■5.NBT.A.3 Conceptual, Procedural | Read, write, and compare decimals to thousandths. | fractions (4.NF.C) to support entry into understanding the place value system with | |
| 4.NBT.A.2 | ■5.NBT.A.3a Conceptual, Procedural | Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$. | decimals (5.NBT.A.1, 3, and 4). | |
| | ■5.NBT.A.3b Conceptual | Compare two decimals to thousandths based on meanings of the digits in each place, using >, =, and < symbols to record the results of comparisons. | | |
| 4.NBT.A.3 | ■ 5.NBT.A.4 Conceptual, Procedural | Use place value understanding to round decimals to any place. | | |
| 4.NBT.B.5, 4.OA.A.3 | ■ 5.NBT.B.5 Procedural | Fluently multiply multi-digit whole numbers using the standard algorithm. | Incorporate foundational work on multiplying and dividing multi-digit whole numbers (4.NBT.B.5 & 6) to | |
| 4.NBT.B.6 <u>,</u> 4.OA.A.3 | ■ 5.NBT.B.6 Conceptual, Procedural | Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, subtracting multiples of the divisor and/or the relationship between multiplication and division. Illustrate and/or explain the calculation by using equations, rectangular arrays, area models, or other strategies based on place value. | support students' work | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|---|---|---|---|-------------|
| 4.NF.C.5, 4.NF.C.6, 4.NF.C.7, 4.OA.A.3 | ■5.NBT.B.7 Conceptual, Procedural | Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used; justify the reasoning used with a written explanation. | Incorporate students' understanding of decimal fractions (4.NF.C) to support entry into the grade 5 work of operations with decimals. | |
| 4.NF.A.1 <i>,</i> 4.NF.B.3a-c | ■5.NF.A.1 Conceptual, Procedural | Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, $2/3 + 5/4 = 8/12 + 15/12 = 23/12$. (In general, $a/b + c/d = (ad + bc)/bd$.) | work on equivalent fractions | |
| | ■5.NF.A.2 Application | Solve word problems involving addition and subtraction of fractions. | (4.NF.A.1) and on the conceptual understanding underlying fraction addition (4.NF.B.3) and to support students' work on adding and subtracting fractions with unlike denominators | |
| | ■5.NF.A.2a Application | Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. | | |
| | ■5.NF.A.2b Conceptual | Use benchmark fractions and number sense of fractions to estimate mentally and justify the reasonableness of answers. For example, recognize an incorrect result of $2/5 + 1/2 = 3/7$, by observing that $3/7 < 1/2$. | (5.NF.A). | |
| | 5.NF.B.3 Conceptual, Application | Interpret a fraction as division of the numerator by the denominator ($a/b = a \div b$). Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret 3/4 as the result of dividing 3 by 4, noting that 3/4 multiplied by 4 equals 3 and that when 3 wholes are shared equally among 4 people each person has a share of size 3/4. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie? | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|--|--|-------------|
| | ■5.NF.B.4 Conceptual, Procedural | Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction. | | |
| | ■5.NF.B.4a Conceptual | Interpret the product $(m/n) \times q$ as m parts of a partition of q into n equal parts; equivalently, as the result of a sequence of operations, m $\times q \div n$. For example, use a visual fraction model to show understanding, and create a story context for $(m/n) \times q$. | | |
| 4.NF.B.4a-b | ■ 5.NF.B.4b Conceptual | story context for the equation. [In general, $(m/n) \times (c/d) = (mc)/(nd)$.] | Incorporate foundations for multiplying fractions by whole numbers (4.NF.B.4) to support students' work in multiplying fractions and | |
| | ■5.NF.B.4c Conceptual, Procedural | Find the area of a rectangle with fractional side lengths by tiling it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found by multiplying the side lengths. | whole numbers by fractions (5.NF.4). | |
| | ■ 5.NF.B.4d Conceptual, Procedural | Multiply fractional side lengths to find areas of rectangles, and represent fraction products as rectangular areas. | | |
| | ■5.NF.B.5 Conceptual | Interpret multiplication as scaling (resizing), by: | | |
| | ■5.NF.B.5a Conceptual | Comparing the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication. | | |
| 4.OA.A.1, 4.OA.A.2 | ■5.NF.B.5b Conceptual | Explaining why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case). | | |
| | ■5.NF.B.5c Conceptual | Explaining why multiplying a given number by a fraction less than 1 results in a product smaller than the given number. | | |
| | ■5.NF.B.5d Conceptual | Relating the principle of fraction equivalence $a/b = (n \times a) / (n \times b)$ to the effect of multiplying a/b by 1. | | |
| | ■5.NF.B.6 Application | Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|--|---|--|---|
| | ■ 5.NF.B.7 Conceptual, Procedural | Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions. Students able to multiply fractions in general can develop strategies to divide fractions in general, by reasoning about the relationship between multiplication and division. But division of a fraction by a fraction is not a requirement at this grade. | | |
| | ■ 5.NF.B.7a Conceptual, Procedural | Interpret division of a unit fraction by a non-zero whole number, and compute such quotients. For example, create a story context for $(1/3) \div 4$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $(1/3) \div 4 = 1/12$ because $(1/12) \times 4 = 1/3$. | | |
| | ■ 5.NF.B.7b Conceptual, Procedural | Interpret division of a whole number by a unit fraction, and compute such quotients. For example, create a story context for $4 \div (1/5)$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $4 \div (1/5) = 20$ because $20 \times (1/5) = 4$. | | |
| | ■ 5.NF.B.7c Application | Solve real world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. For example, how much chocolate will each person get if 3 people share 1/2 lb of chocolate equally? How many 1/3-cup servings are in 2 cups of raisins? | | |
| 4.MD.A.1 | 5.MD.A.1 Procedural, Application | Convert among different-sized standard measurement units within a given measurement system and use these conversions in solving multi-step real world problems (e.g., convert 5 cm to 0.05 m). | Combine lessons on converting measurement units in order to reduce the amount of time spent on this topic. | 1.4 2.13, 2.14, 2.15 4.9, 4.19, 4.20 5.5 (E) |
| | ■ 5.MD.B.2 Application | Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Use operations on fractions for this grade to solve problems involving information presented in line plots. For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally. | Eliminate lessons and problems on representing and interpreting data using line plots that do not strongly reinforce the fraction work of this grade (5.NF). | 4.1, 4.10 |
| | ■5.MD.C.3 Conceptual | Recognize volume as an attribute of solid figures and understand concepts of volume measurement. | | |
| | 5.MD.C.3a Conceptual | A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|---|--|---|---|
| | ■5.MD.C.3b Conceptual | A solid figure which can be packed without gaps or overlaps using <i>n</i> unit cubes is said to have a volume of <i>n</i> cubic units. | | |
| | ■5.MD.C.4 Procedural | Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units. | | |
| | ■5.MD.C.5 Conceptual, Application, Procedural | Relate volume to the operations of multiplication and addition and solve real world and mathematical problems involving volume. | | |
| | ■5.MD.C.5a Conceptual, Procedural | Find the volume of a right rectangular prism with whole-number side lengths by packing it with unit cubes, and show that the volume is the same as would be found by multiplying the edge lengths, equivalently by multiplying the height by the area of the base. Represent threefold whole-number products as volumes, e.g., to represent the associative property of multiplication. | | |
| | ■ 5.MD.C.5b Procedural, Application | Apply the formulas V = I x w x h and V = b x h for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving real world and mathematical problems. | | |
| | ■5.MD.C.5c Conceptual, Procedural, Application | Recognize volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms by adding the volumes of the non-overlapping parts, applying this technique to solve real world problems. | | |
| | •5.G.A.1 Conceptual | Use a pair of perpendicular number lines, called axes, to define a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plane located by using an ordered pair of numbers, called its coordinates. Understand that the first number in the ordered pair indicates how far to travel from the origin in the direction of one axis, and the second number in the ordered pair indicates how far to travel in the direction of the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., <i>x</i> -axis and <i>x</i> -coordinate, <i>y</i> -axis and <i>y</i> -coordinate). | Incorporate foundational understandings of number lines (such as found in the work of 4.NF) into the work of extending number lines to the coordinate plane, as detailed in this cluster. Emphasize interpreting coordinate values of points in the context of a situation. | 6.2, 6.3, 6.3, 6.5 (E), 6.6 (E), 6.7, 6.8, 6.9, 6.10 (E), 6.11 (E), 6.12 (E), 6.13 (E), 6.14 (E), 6.15 (E), 6.16, 6.17 (E), 6.18 (E), 6.20 |
| | •5.G.A.2 Conceptual, Procedural | Represent real world and mathematical problems by graphing points in the first quadrant of the coordinate plane, and interpret coordinate values of points in the context of the situation. | | 6.4 (E), 6.6 (E), 6.7, 6.8, 6.9, 6.10 (E), 6.11 (E), 6.12 (E), 6.13 (E), 6.14 (E), 6.15 (E), 6.16, 6.17 (E), 6.18 (E), 6.19, 6.20 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math |
|--------------------------|-------------------------|---|--|---------------------------------------|
| 4.G.A.1, 4.G.A.2 | | subcategories of that category. For example, all rectangles have four right angles and squares are rectangles, so all squares have four right angles. | dimensional figures into categories based on properties in order to reduce the amount of time | 5.16, 5.17, 5.18, 5.19, 5.21 |
| | 0.0.01 | Classify quadrilaterals in a hierarchy based on properties. (Students will define a trapezoid as a quadrilateral with at least one pair of parallel sides.) | | 5.16, 5.17, 5.18, 5.19, 5.20, 5.21 |



| | Grade 6 Math Important Prerequisites | | | | | | |
|--|---|--|---|--|---|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade- Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per SAP quidance | Comments related to widely used Tier 1 Curriculum Eureka Math | Comments related to widely used Tier 1 Curriculum Illustrative Math | | |
| 5.NF.B.5a-b | ■6.RP.A.1 Conceptual | Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes." | | | | | |
| 5.NF.B.3 5.NF.B.5a-b | ■6.RP.A.2 Conceptual | Understand the concept of a unit rate a/b associated with a ratio a:b with b not equal to 0, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is 3/4 cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger." | | | | | |
| | ■6.RP.A.3 Application, Procedural | Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. | | | | | |
| 5.G.A.1, 5.G.A.2 | ■6.RP.A.3a Conceptual, Procedural | Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios. | | | | | |
| | ■6.RP.A.3b Application | Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what rate were lawns being mowed? | | | | | |
| | ■6.RP.A.3c Procedural, Application | Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means 30/100 times the quantity); solve problems involving finding the whole, given a part and the percent. | | | | | |
| | ■6.RP.A.3d Conceptual, Procedural | Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities. | | | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---|---|---|------------------------------------|--|
| 5.NF.B.7a-b | ■ 6.NS.A.1 Conceptual, Procedural, Application | Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for $(2/3) \div (3/4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $(2/3) \div (3/4) = 8/9$ because $3/4$ of $8/9$ is $2/3$. [In general, $(a/b) \div (c/d) = ad/bc$.] How much chocolate will each person get if 3 people share $1/2$ lb of chocolate equally? How many $3/4$ -cup servings are in $2/3$ of a cup of yogurt? How wide is a rectangular strip of land with length $3/4$ mi and area $1/2$ square mi? | | | |
| 5.NBT.B.6 | •6.NS.B.2 Procedural | Fluently divide multi-digit numbers using the standard algorithm. | Eliminate lessons on computing fluently by integrating these problems into spiraled practice throughout the year. Time should not be spent remediating multi- digit calculation algorithms. | 2.12, 2.13, 2.14, 2.15 (E) | 6.5.9, 6.5.10, 6.5.11 |
| 5.NBT.B.7 | •6.NS.B.3 Procedural | Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation. | | 2.9, 2.10, 2.11, 2.14, 2.15 (E) | 6.5.2, 6.5.3, 6.5.4, 6.5.7, 6.5.8, 6.5.12, 6.5.13, 6.5.14, 6.5.15, 6.6.4, 6.8.12, 6.9.6 |
| | • 6.NS.B.4 Procedural | Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express $36 + 8$ as $4 (9 + 2)$. | | | |
| | ■6.NS.C.5 Conceptual | Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation. | | | |
| | ■6.NS.C.6 Conceptual | Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|--|--|--------------------|-------------|----------------------|
| | ■6.NS.C.6a Conceptual | Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., $-(-3) = 3$, and that 0 is its own opposite. | | | |
| | ■6.NS.C.6b Conceptual | Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes. | | | |
| | ■6.NS.C.6c Conceptual, Procedural | Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane. | | | |
| | ■6.NS.C.7 Conceptual | Understand ordering and absolute value of rational numbers. | | | |
| | ■6.NS.C.7a Conceptual | Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. For example, interpret -3 > -7 as a statement that -3 is located to the right of -7 on a number line oriented from left to right. | | | |
| | ■6.NS.C.7b Conceptual, Application | Write, interpret, and explain statements of order for rational numbers in real-world contexts. <i>For example, write -3C > -7C to express the fact that -3C is warmer than -7C.</i> | | | |
| | 6.NS.C.7c Conceptual, Application | Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation. For example, for an account balance of -30 dollars, write -30 = 30 to describe the size of the debt in dollars. | | | |
| | ■6.NS.C.7d Conceptual | Distinguish comparisons of absolute value from statements about order. For example, recognize that an account balance less than –30 dollars represents a debt greater than 30 dollars. | | | |
| 5.G.A.1, 5.G.A.2 | ■6.NS.C.8 Application, Procedural | Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate. | | | |
| 5.NBT.A.2 | ■6.EE.A.1 Procedural, Conceptual | Write and evaluate numerical expressions involving whole-number exponents. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|------------------------------------|---|--|--------------------|-------------|----------------------|
| | 6.EE.A.2 Procedural, Conceptual | Write, read, and evaluate expressions in which letters stand for numbers. | | | |
| | ■6.EE.A.2a Conceptual | Write expressions that record operations with numbers and with letters standing for numbers. <i>For example, express the calculation "Subtract y from 5" as 5 - y.</i> | | | |
| 5.0A.A.1, 5.0A.A.2, 5.0A.B.3 | ■6.EE.A.2b Procedural, Conceptual | Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); view one or more parts of an expression as a single entity. For example, describe the expression 2(8 + 7) as a product of two factors; view (8 + 7) as both a single entity and a sum of two terms. | | | |
| | ■6.EE.A.2c Procedural | Evaluate expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. Perform arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas $V = s^3$ and $A = 6 s^2$ to find the volume and surface area of a cube with sides of length $s = 1/2$. | | | |
| | ■6.EE.A.3 Procedural, Conceptual | Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression 3 $(2 + x)$ to produce the equivalent expression 6 + 3x; apply the distributive property to the expression $24x + 18y$ to produce the equivalent expression 6 $(4x + 3y)$; apply properties of operations to $y + y + y$ to produce the equivalent expression 3y. | | | |
| | ■6.EE.A.4 Conceptual | Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y + y + y$ and $3y$ are equivalent because they name the same number regardless of which number y stands for. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|--|---|--------------------|-------------|----------------------|
| | ■6.EE.B.5 Conceptual, Procedural | Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true. | | | |
| 5.NF.A.1, 5.NF.A.2, | ■6.EE.B.6 Conceptual, Application, Procedural | Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. | | | |
| 5.NF.B.4a-b, 5.NF.B.6 | ■6.EE.B.7 Application, Procedural | Solve real-world and mathematical problems by writing and solving equations and inequalities of the form $x + p = q$ and $px = q$ for cases in which p, q and x are all nonnegative rational numbers. Inequalities will include <, >, ≤, and ≥ | | | |
| | ■6.EE.B.8 Conceptual, Procedural | Write an inequality of the form x > c or x < c to represent a constraint or condition in a real- world or mathematical problem. Recognize that inequalities of the form x > c or x < c have infinitely many solutions; represent solutions of such inequalities on number line diagrams. | | | |
| | ■6.EE.C.9 Conceptual, Procedural | Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation d = 65t to represent the relationship between distance and time. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|--|---|--|--|--|
| | ■ 6.G.A.1 Conceptual, Procedural, Application | Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems. | Emphasize understanding of the reasoning leading to the triangle area formula. Instead of teaching additional area formulas as separate topics, emphasize problems that focus on finding areas in real-world problems by decomposing figures into triangles and rectangles. | 5.1, 5.2, 5.3, 5.4, 5.5, 5.6, 5.8, 5.9, 5.10 | 6.1.2, 6.1.3, 6.1.4, 6.1.5, 6.1.6, 6.1.7, 6.1.8, 6.1.9, 6.1.10, 6.1.11, 6.1.19, 6.4.14 |
| 5.MD.C.4, 5.MD.C.5a-c | 6.G.A.2 Conceptual, Procedural, Application | Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas V = I w h and V = b h to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems. | Emphasize contextual problems, as detailed in the second sentence of the standard; eliminate lessons focused on the first sentence of the standard (finding the volume of a rectangular prism with fractional edge lengths by packing it with unit cubes). | 5.11, 5.12, 5.13, 5.14, 5.19 | 6.1.15, 6.4.14, 6.4.15, 6.4.17 |
| 5.G.A.1, 5.G.A.2 | 6.G.A.3 Conceptual, Application, Procedural | Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems. | Eliminate lessons and problems involving polygons on the coordinate plane. | 5.7, 5.8, 5.9, 5.10 | 6.7.15 |
| | ■ 6.G.A.4 Conceptual, Application, Procedural | Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems. | Eliminate lessons and problems on constructing three- dimensional figures from nets and determining if nets can be constructed into three- dimensional figures during the study of nets and surface area. | 5.15, 5.16, 5.17, 5.19, 5.19a (E) | 6.1.12, 6.1.13, 6.1.14, 6.1.15, 6.1.16, 6.1.18, 6.1.19 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---|--|--|--|---|
| | ○6.SP.A.1 Conceptual | Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages. | | 6.1, 6.17, 6.20, 6.21, 6.22 | 6.8.2, 6.8.3, 6.8.6, 6.8.7, 6.8.17 |
| | 6.SP.A.2 Conceptual | Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape. | Combine lessons about introductory statistical concepts so as to proceed more quickly to applying and reinforcing these concepts in context. | 6.2, 6.3, 6.4, 6.5 (E), 6.6, 6.7 (R), 6.8, 6.9 (E), 6.10 (E), 6.11 (E), 6.12, 6.13, 6.14, 6.15, 6.16, 6.17, 6.18, 6.19 (E), 6.20, 6.21, 6.22 | 6.8.4, 6.8.5, 6.8.7, 6.8.8, 6.8.11, 6.8.18 |
| | •6.SP.A.3 Conceptual | Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number. | | 6.6, 6.7 (R), 6.8, 6.9 (E), 6.10 (E), 6.11 (E), 6.12, 6.13, 6.14, 6.15, 6.16 | 6.8.6, 6.8.9, 6.8.10, 6.8.11 |
| | ○6.SP.B.4 Procedural | Display numerical data in plots on a number line, including dot plots, histograms, and box plots. | | 6.2, 6.3, 6.4, 6.5, 6.6, 6.7 (R), 6.8, 6.10 (E), 6.11 (E), 6.14, 6.15, 6.18, 6.20, 6.21, 6.22 | 6.8.3, 6.8.4, 6.8.5, 6.8.6, 6.8.7, 6.8.8, 6.8.16, 6.8.17 |
| | 6.SP.B.5 Conceptual, Procedural | Summarize numerical data sets in relation to their context, such as by: | Reduce the amount of required student practice in calculating | See alignment for 6.SP.B.5a-d | 6.8.17 |
| | •6.SP.B.5a Conceptual | Reporting the number of observations. | measures of center and measures of variation by hand, to emphasize the concept of a distribution and the usefulness of summary measures. Reduce the amount of time spent creating data displays by hand. | 6.5 (E), 6.12, 6.13, 6.16, 6.20, 6.21, 6.22 | 6.8.3, 6.8.4 |
| | 6.SP.B.5b Conceptual | Describing the nature of the attribute under investigation, including how it was measured and its units of measurement. | | 6.13, 6.20, 6.21, 6.22 | 6.8.2, 6.8.3, 6.8.5, 6.8.6, 6.8.7, 6.8.14 |
| | •6.SP.B.5c Conceptual, Procedural | Giving quantitative measures of center (median and/or mean) and variability (interquartile range), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the context in which the data were gathered. | | 6.10 (E), 6.11 (E), 6.12, 6.13, 6.14, 6.15, 6.16, 6.20, 6.21, 6.22 | 6.8.9, 6.8.10, 6.8.11, 6.8.12, 6.8.13, 6.8.14, 6.8.15, 6.8.16, 6.8.18 |
| | 6.SP.B.5d Conceptual | Relating the choice of measures of center and variability to the shape of the data distribution and the context in which the data were gathered. | | 6.20, 6.21, 6.22 | 6.8.12, 6.8.14, 6.8.15, 6.8.16, 6.8.18 |



| | Grade 7 Math Important Prerequisites | | | | | | | | |
|--|--|---|--|---|---|--|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP guidance</u> | Comments related to widely used Tier 1 Curriculum Eureka Math | Comments related to widely used Tier 1 Curriculum Illustrative Math | | | | |
| | ■7.RP.A.1 Procedural | Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units. For example, if a person walks $1/2$ mile in each $1/4$ hour, compute the unit rate as the complex fraction $(1/2)/(1/4)$ miles per hour, equivalently 2 miles per hour. | | | | | | | |
| 6.EE.C.9, | ■7.RP.A.2 Conceptual, Procedural | Recognize and represent proportional relationships between quantities. | | | | | | | |
| 6.RP.A.1, 6.RP.A.2, 6.RP.A.3a-c, | ■7.RP.A.2a Conceptual, Procedural | Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin. | | | | | | | |
| 6.RP.A.3d | ■7.RP.A.2b Conceptual | Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. | | | | | | | |
| | ■7.RP.A.2c Conceptual, Procedural | Represent proportional relationships by equations. For example, if total cost t is proportional to the number n of items purchased at a constant price p, the relationship between the total cost and the number of items can be expressed as $t = pn$. | | | | | | | |
| | ■7.RP.A.2d Conceptual | Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points (0, 0) and (1, r) where r is the unit rate. | | | | | | | |
| | ■7.RP.A.3 Procedural, Application | Use proportional relationships to solve multistep ratio and percent problems of simple interest, tax, markups and markdowns, gratuities and commissions, fees, percent increase and decrease, percent error. | | | | | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--|--|--|--------------------|-------------|----------------------|
| | ■7.NS.A.1 Conceptual, Procedural | Apply and extend previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram. | | | |
| | ■7.NS.A.1a Conceptual, Application | Describe situations in which opposite quantities combine to make 0. <i>For example, a hydrogen atom has 0 charge because its two constituents are oppositely charged.</i> | | | |
| 6.NS.B.3, 6.NS.C.6a, 6.NS.C.6c, 6.NS.C.7a-d | ■7.NS.A.1b Conceptual, Application | Understand p + q as the number located a distance q from p, in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts. | | | |
| | ■7.NS.A.1c Conceptual, Application | Understand subtraction of rational numbers as adding the additive inverse, $p - q = p + (-q)$. Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts. | | | |
| | ■7.NS.A.1d Conceptual, Procedural | Apply properties of operations as strategies to add and subtract rational numbers. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|---------------------------------------|---|---|--------------------|-------------|----------------------|
| | ■7.NS.A.2 Conceptual, Procedural | Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers. | | | |
| | ■7.NS.A.2a Conceptual | Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as (-1)(-1) = 1 and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts. | | | |
| 6.NS.A.1, 6.NS.B.3 | 7.NS.A.2b Conceptual | Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers, then $-(p/q) = (-p)/q = p/(-q)$. Interpret quotients of rational numbers by describing real-world contexts. | | | |
| | ■7.NS.A.2c Conceptual, Procedural | Apply properties of operations as strategies to multiply and divide rational numbers. | | | |
| | ■7.NS.A.2d Conceptual, Procedural | Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats. | | | |
| | 7.NS.A.3 Procedural, Application | Solve real-world and mathematical problems involving the four operations with rational numbers.* *Computations with rational numbers extend the rules for manipulating fractions to complex fractions. | | | |
| 6.EE.A.2a-b, 6.EE.A.3, 6.EE.A.4 | ■7.EE.A.1 Conceptual, Procedural | Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients to include multiple grouping symbols (e.g., parentheses, brackets, and braces). | | | |
| | ■7.EE.A.2 Conceptual | Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related. For example, $a + 0.05a = 1.05a$ means that "increase by 5%" is the same as "multiply by 1.05." | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|------------------------------------|---|---|---|---|--|
| | ■7.EE.B.3 Conceptual, Procedural, Application | Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form (whole numbers, fractions, and decimals), using tools strategically. Apply properties of operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies. <i>For example: If a woman making \$25 an hour gets a 10% raise, she will make an additional 1/10 of her salary an hour, or \$2.50, for a new salary of \$27.50. If you want to place a towel bar 9 3/4 inches long in the center of a door that is 27 1/2 inches wide, you will need to place the bar about 9 inches from each edge; this estimate can be used as a check on the exact computation.</i> | | | |
| | ■ 7.EE.B.4 Conceptual, Procedural, Application | Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities. | | | |
| 6.EE.B.5, 6.EE.B.6, 6.EE.B.7 | ■7.EE.B.4a Conceptual, Procedural, Application | Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where p, q, and r are specific rational numbers. Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, The perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width? | Emphasize equations (7.EE.B.4a) relative to inequalities (7.EE.B.4b). | | |
| 6.EE.B.8 | ■7.EE.B.4b Conceptual, Procedural, Application | Solve word problems leading to inequalities of the form $px+q>r$, $px + q \ge r$, $px + q < r$, or $px + q \le r$, where p, q, and r are specific rational numbers. Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid \$50 per week plus \$3 per sale. This week you want your pay to be at least \$100. Write an inequality for the number of sales you need to make, and describe the solutions. | | | |
| 6.G.A.1 <i>,</i> 6.G.A.3 | •7.G.A.1 Procedural, Application | Solve problems involving scale drawings of geometric figures, such as computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale. | Reduce time spent creating scale drawings by hand. | 1.16, 1.17, 1.18, 1.19, 1.20 (E), 1.21, 1.22 4.12, 4.13, 4.14, 4.15 | 7.1.1, 7.1.2, 7.1.3, 7.1.4, 7.1.5, 7.1.6, 7.1.7, 7.1.8, 7.1.9, 7.1.10, 7.1.11, 7.1.12, 7.1.13, 7.2.1, 7.3.6, 7.3.11, 7.9.4, 7.9.13 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|---------------------------------|--|--|--|---|--|
| | •7.G.A.2 Conceptual, Procedural | Draw (freehand, with ruler and protractor, or with technology) geometric shapes with given conditions. (Focus is on triangles from three measures of angles or sides, noticing when the conditions determine one and only one triangle, more than one triangle, or no triangle.) | Eliminate lessons on drawing and constructing triangles as detailed in this standard. | 6.6, 6.7, 6.8, 6.9, 6.10, 6.11, 6.12 | 7.3.2, 7.7.6, 7.7.7, 7.7.8, 7.7.9, 7.7.10, 7.7.17 |
| | •7.G.A.3 Conceptual | Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids. | Eliminate lessons on analyzing figures that result from slicing three- dimensional figures as detailed in this standard. | 6.16, 6.17, 6.18 | 7.7.11, 7.7.13 |
| | • 7.G.B.4 Conceptual, Procedural, Application | Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle. | Combine lessons on knowing and using the formulas for the area and circumference of a circle in order to reduce the amount of time spent on this topic. Limit the amount of required student practice. | 3.16, 3.17, 3.18, 3.20 6.22 | 7.3.3, 7.3.4, 7.3.5, 7.3.7, 7.3.8, 7.3.9, 7.3.10, 7.3.11, 7.9.4, 7.9.11, 7.9.12 |
| | •7.G.B.5 Conceptual, Procedural | Use facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure. | Combine lessons to address key concepts and skills of unknown | 3.10, 3.11 6.1, 6.2, 6.3, 6.4 | 7.7.2, 7.7.3, 7.7.4, 7.7.5 |
| 6.G.A.1, 6.G.A.2, 6.G.A.4 | •7.G.B.6 Procedural, Application | Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms. (Pyramids limited to surface area only.) | Reduce the amount of required student practice. Do not require | 3.19, 3.20, 3.21, 3.22, 3.23, 3.24, 3.25, 3.26 6.20, 6.23, 6.24, 6.25, 6.26, 6.27 | 7.1.6, 7.2.8, 7.3.6, 7.7.12, 7.7.13, 7.7.14, 7.7.15, 7.7.16, 7.7.17, 7.9.4, 7.9.5, 7.9.9 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---|---|---|---------------------------------------|--|
| 6.SP.A.1 | Conceptual | Understand that statistics can be used to gain information about a population by examining a sample of the population; generalizations about a population from a sample are valid only if the sample is representative of that population. Understand that random sampling tends to produce representative samples and support valid inferences. | Combine lessons on using random sampling to draw inferences about a population and using measures of center and | 5.13, 5.14, 5.15, 5.16 | 7.8.12, 7.8.13, 7.8.14, 7.8.15, 7.8.20 |
| | 7.SP.A.2 Procedural, Conceptual, Application | to gauge the variation in estimates or predictions. For example, estimate the mean word length in a book by randomly sampling words from the book; predict the winner of a school election based on randomly sampled survey data. Gauge how far off the estimate or | variability to draw comparative inferences about two populations in order to reduce the amount of time spent on this topic. Limit the amount of required student practice. | 5.15, 5.16, 5.17, 5.18, 5.19, 5.20 | 7.8.13, 7.8.14, 7.8.15, 7.8.16, 7.8.17, 7.8.20 |
| 6.SP.A.1, 6.SP.A.2 | •7.SP.B.3 Conceptual, | variability (interquartile range and/or mean absolute deviation), as well as describing any overall pattern and any striking deviations from the overall pattern with reference to the | | 5.15, 5.16, 5.17, 5.18, 5.19, 5.20 | 7.8.11, 7.8.18 |
| | Procedural, Conceptual, | Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations. <i>For example, decide whether the words in a chapter of a seventh-grade science book are generally longer than the words in a chapter of a fourth-grade science book.</i> | | 5.21, 5.22, 5.23 | 7.8.15, 7.8.16, 7.8.18, 7.8.19, 7.8.20, 7.9.3 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math | | |
|--------------------------|--|---|---|-------------------------|--------------------------------------|-------------------------|--------------------------------------|
| | 7.SP.C.5 Conceptual | Understand that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring. Larger numbers indicate greater likelihood. A probability near 0 indicates an unlikely event, a probability around 1/2 indicates an event that is neither unlikely nor likely, and a probability near 1 indicates a likely event. | - | | | 5.1, 5.2, 5.3, 5.4, 5.5 | 7.8.2, 7.8.3, 7.8.4, 7.8.5, 7.8.6 |
| | 7.SP.C.6 Conceptual, Procedural | Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability. <i>For example, when rolling a number cube 600 times, predict that a 3 or 6 would be rolled roughly 200 times, but probably not exactly 200 times.</i> | | 5.2, 5.3, 5.4, 5.8, 5.9 | 7.8.1, 7.8.3, 7.8.4, 7.8.5, 7.8.6 | | |
| | 7.SP.C.7 Conceptual, Procedural | Develop a probability model and use it to find probabilities of events. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy. | concepts and reduce the | 5.5, 5.10, 5.12 | 7.8.3, 7.8.4, 7.8.5, 7.8.14 | | |
| | 7.SP.C.7a Conceptual, Procedural | Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events. <i>For example, if a student is selected at</i> <i>random from a class, find the probability that Jane will be selected and the probability that a</i> <i>girl will be selected.</i> | amount of required student practice. | 5.4, 5.10, 5.12 | 7.8.3, 7.8.20 | | |
| | 7.SP.C.7b Conceptual, Procedural | Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process. For example, find the approximate probability that a spinning penny will land heads up or that a tossed paper cup will land open-end down. Do the outcomes for the spinning penny appear to be equally likely based on the observed frequencies? | | 5.10, 5.12 | 7.8.4, 7.8.5, 7.8.6 | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|--|--|--|----------------------------------|----------------------------------|
| | 7.SP.C.8 Procedural, Conceptual, Application | Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation. | Eliminate lessons and problems on finding probabilities of compound events as detailed in this standard. | See alignment for 7.SP.C.8a-c | See alignment for 7.SP.C.8a-c |
| | 7.SP.C.8a Conceptual | Understand that, just as with simple events, the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs. | | 5.10, 5.11, 5.12 | 7.8.9 |
| | 7.SP.C.8b Conceptual, Application | and tree diagrams. For an event described in everyday language (e.g., "rolling double sixes"), | | 5.6 (E), 5.7 (E), 5.10, 5.12 | 7.8.8, 7.8.9 |
| | 7.SP.C.8c Procedural, Conceptual, Application | Design and use a simulation to generate frequencies for compound events. For example, use random digits as a simulation tool to approximate the answer to the question: If 40% of donors have type A blood, what is the probability that it will take at least 4 donors to find one with type A blood? | | 5.10, 5.11, 5.12 | 7.8.6, 7.8.7, 7.8.10 |



| | Grade 8 Math Important Prerequisites | | | | | | | | | |
|---|--|--|--|--|---|--|--|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade-Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP guidance</u> | Comments related to widely used Tier 1 Curriculum Eureka Math | Comments related to widely used Tier 1 Curriculum Illustrative Math | | | | | |
| 7.NS.A.1a-d, | 8.NS.A.1 Conceptual, Procedural | Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number. | Integrate irrational numbers with students' | 7.8, 7.10 | 8.8.14, 8.8.15 | | | | | |
| 7.NS.A.2a-d | 8.NS.A.2 Conceptual, Procedural | Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., pi^2). For example, by truncating the decimal expansion of sqrt(2), show that sqrt(2) is between 1 and 2, then between 1.4 and 1.5, and explain how to continue on to get better approximations. | (8.EE.A.Z) unu the | 7.1, 7.2, 7.9, 7.11, 7.13, 7.14 (E) | 8.8.1, 8.8.4, 8.8.5, 8.8.12, 8.8.13 | | | | | |
| | ■8.EE.A.1 Conceptual, Procedural | Know and apply the properties of integer exponents to generate equivalent numerical expressions. For example, $3^2 \times 3^{-5} = 3^{-3} = 1/3^3 = 1/27$. | | | | | | | | |
| | 8.EE.A.2 Conceptual, Procedural | Use square root and cube root symbols to represent solutions to equations of the form $x^2 = p$ and $x^3 = p$, where p is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that sqrt(2) is irrational. | Eliminate lessons and problems about cube roots. | 7.2, 7.3, 7.5 | 8.7.2, 8.7.3, 8.7.4, 8.7.5, 8.7.6, 8.7.7, 8.7.8, 8.7.11, 8.7.14 | | | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--|---|--|--|-------------------------------------|---|
| | ■8.EE.A.3 Conceptual, Procedural | Use numbers expressed in the form of a single digit times an integer power of 10 to estimate very large or very small quantities, and to express how many times as much one is than the other. For example, estimate the population of the United States as 3×10^{-8} and the population of the world as 7×10^{-9} , and determine that the world population is more than 20 times larger. | Eliminate lessons and practice dedicated to calculating with scientific notation, but include examples of numbers expressed in scientific | 1.8, 1.9, 1.11, 1.12, 1.13 | 8.7.9, 8.7.10, 8.7.11, 8.7.12, 8.7.14, 8.7.16 |
| 7.EE.B.3 | ■ 8.EE.A.4 Conceptual, Procedural | Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Use scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology. | | 1.8, 1.9, 1.10, 1.11, 1.12, 1.13 | 8.7.10, 8.7.11, 8.7.12, 8.7.13, 8.7.14, 8.7.15, 8.7.16 |
| 7.RP.A.1 <i>,</i> 7.RP.A.2a-d | 8.EE.B.5 Procedural, Conceptual, Application | Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed. | | | |
| 7.G.A.1, 7.RP.A.1, 7.RP.A.2a-d | ■8.EE.B.6 Conceptual | Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation $y = mx$ for a line through the origin and the equation $y = mx + b$ for a line intercepting the vertical axis at b. | | | |
| | ■8.EE.C.7 Procedural | Solve linear equations in one variable. | | | |
| 7.EE.A.1, 7.NS.A.1a-d, 7.NS.A.2a-d | 8.EE.C.7a Conceptual, Procedural | Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form $x = a$, $a = a$, or $a = b$ results (where a and b are different numbers). | | | |
| | ■8.EE.C.7b Procedural | Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---|---|--|------------------|-----------------------|
| | 8.EE.C.8 Conceptual, Procedural | Analyze and solve pairs of simultaneous linear equations. | | | |
| | ■8.EE.C.8a Conceptual | Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously. | | | |
| 7.EE.B.4a | 8.EE.C.8b Conceptual, Procedural | Solve systems of two linear equations in two variables algebraically, and estimate solutions by graphing the equations. Solve simple cases by inspection. For example, $3x + 2y = 5$ and $3x + 2y = 6$ have no solution because $3x + 2y$ cannot simultaneously be 5 and 6. | Limit the amount of required student practice in solving systems algebraically. | 4.24, 4.27, 4.28 | <u>8.4.12, 8.4.15</u> |
| | 8.EE.C.8c Procedural, Application | Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair. | | | |
| | ■8.F.A.1 Conceptual | Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output. (Function notation is not required in this grade level.) | | | |
| | 8.F.A.2 Conceptual, Application | Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change. | | | |
| | ■ 8.F.A.3 Conceptual, Procedural | Interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line; categorize functions as linear or nonlinear when given equations, graphs, or tables. For example, the function $A = s^2$ giving the area of a square as a function of its side length is not linear because its graph contains the points (1,1), (2,4) and (3,9), which are not on a straight line. | | | |
| | ■ 8.F.B.4 Conceptual, Procedural | Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---------------------------------------|--|--|-----------------------------------|---|
| | ■8.F.B.5 Conceptual | Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally. | | | |
| | ■8.G.A.1 Conceptual | Verify experimentally the properties of rotations, reflections, and translations: | | | 8.1.2, 8.1.3, 8.1.4, 8.1.6, 8.1.11, 8.1.14, 8.3.8 |
| | ■8.G.A.1a Conceptual | Lines are taken to lines, and line segments to line segments of the same length. | | 2.1, 2.2, 2.3, 2.4, | 8.1.7, 8.1.8, 8.1.9, 8.1.10, 8.1.13 |
| | ■8.G.A.1b Conceptual | Angles are taken to angles of the same measure. | | 2.5, 2.6 | 8.1.7, 8.1.8, 8.1.9, 8.1.10 |
| | ■8.G.A.1c Conceptual | Parallel lines are taken to parallel lines. | | | 8.1.9 |
| | ■8.G.A.2 Conceptual, Procedural | Explain that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them. (Rotations are only about the origin and reflections are only over the y-axis and x-axis in grade 8.) | Combine lessons to address key concepts in congruence and combine | 2.1, 2.7, 2.8, 2.9, 2.10, 2.11 | 8.1.11, 8.1.12, 8.1.13, 8.1.15, 8.2.6, 8.2.7 |
| | 8.G.A.3 Conceptual | Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates. (Rotations are only about the origin, dilations only use the origin as the center of dilation, and reflections are only over the y-axis and x-axis in grade 8.) | lessons to address key concepts in similarity of two-dimensional figures in order to reduce the | 2.6, 3.5, 3.6 | 8.1.5, 8.1.6, 8.2.4, 8.2.5, 8.2.12 |
| | ■8.G.A.4 Conceptual, Procedural | Explain that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two- dimensional figures, describe a sequence that exhibits the similarity between them. (Rotations are only about the origin, dilations only use the origin as the center of dilation, and reflections are only over the y-axis and x-axis in grade 8.) | τορις. | 3.1, 3.8, 3.9 | 8.2.6, 8.2.7, 8.2.9 |
| 7.G.B.5 | ■8.G.A.5 Conceptual | Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. For example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so. | | 2.12, 2.13, 2.14, 3.10 | 8.1.14, 8.1.15, 8.1.16, 8.2.8, 8.2.13, 8.9.2 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|--------------------------|---|--|--|---------------------------------|--|
| | ■8.G.B.6 Conceptual | Explain a proof of the Pythagorean Theorem and its converse using the areas of squares. | | | |
| 7.G.B.6 | ■8.G.B.7 Procedural, Application | Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real- world and mathematical problems in two and three dimensions. | | | |
| | ■8.G.B.8 Procedural | Apply the Pythagorean Theorem to find the distance between two points in a coordinate system. | Eliminate lessons and problems dedicated to applying the Pythagorean Theorem to find the distance between two points in a coordinate system. | 2.16, 7.17 | 8.8.7, 8.8.9 |
| 7.G.B.4, 7.G.B.6 | •8.G.C.9 Conceptual, Procedural, Application | Know the formulas for the volume of cones, cylinders, and spheres and use them to solve real world and mathematical problems. | Combine lessons to address key concepts with volume, with an emphasis on cylinders, in order to reduce the amount of time on this topic. | 5.10, 5.11, 7.19, 7.20, 7.21 | 8.8.6, 8.8.7, 8.8.8, 8.8.10 |
| | 8.SP.A.1 Conceptual, Procedural | Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. | Combine lessons for 8.SP.A.1, 2, and 4 to address key statistical concepts in order to | 6.6, 6.7, 6.10, 6.11 | 8.6.1, 8.6.2, 8.6.3, 8.6.4, 8.6.5, 8.6.6, 8.6.7, 8.6.8 |
| | 8.SP.A.2 Conceptual | Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line. | reduce the amount of time on this topic. Limit the amount of required student practice. Emphasize using linear functions to model association in bivariate | 6.8, 6.9, 6.10, 6.11 | 8.6.6, 8.6.8 |
| | 8.SP.A.3 Conceptual, Application | Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height. | | 6.9, 6.10, 6.11 | |



| Prerequisite Grade-Level Standard Standard | Standard Language | Instructional Time | Eureka Math | Illustrative Math |
|---|--|---|-------------|----------------------|
| 8.SP.A.4 Conceptual, Procedural, Application | subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. <i>For example, collect data from students in your class</i> | Combine lessons for 8.SP.A.1, 2, and 4 to address key statistical concepts in order to reduce the amount of time on this topic. Limit the amount of required student practice. | 6.13, 6.14 | 8.6.9, 8.6.10 |



Algebra I Important Prerequisites

| | Algebra i important Prerequisites | | | | | | | | |
|---|---|---|---|--|--|--|--|--|--|
| Prerequisite Standard Bridge up or heavy traffic from previous grade | Grade- Level Standard Major Supporting Additional | Standard Language | Instructional Time Preserve or reduce time in 20-21 as compared to a typical year, per <u>SAP guidance</u> | Comments related to widely used Tier 1 Curriculum Eureka Math | Comments related to widely used Tier 1 Curriculum SpringBoard | | | | |
| 8.NS.A.1, 8.NS.A.2 | •A1:N.RN.B.3 Conceptual | Explain why the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational. | Reduce focus on this standard in the listed lessons. | 4.13 | 20-2, 20-3 | | | | |
| | A1: N.Q.A.1 Conceptual | Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays. | | | | | | | |
| | A1: N.Q.A.2 Conceptual | Define appropriate quantities for the purpose of descriptive modeling. | | | | | | | |
| | A1: N.Q.A.3 Conceptual | Choose a level of accuracy appropriate to limitations on measurement when reporting quantities. | | | | | | | |
| | A1: A.SSE.A.1 Conceptual | Interpret expressions that represent a quantity in terms of its context. | | | | | | | |
| | ■A1: A.SSE.A.1a Conceptual | Interpret parts of an expression, such as terms, factors, and coefficients. | | | | | | | |
| | | Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret P(1+r)n as the product of P and a factor not depending on P. | Reduce overall emphasis, but retain focus on interpreting expressions to shed light on a quantity in context (as described in parent standard A-SSE.A.1). | 3.2, 3.3, 3.21, 4.3, 4.4 | 2-5 | | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--------------------------|---|--|--|---|--|
| 8.EE.A.2 | ■A1: A.SSE.A.2 Conceptual, Procedural | Use the structure of an expression to identify ways to rewrite it. For example, see $x^4 - y^4$ as $(x^2)^2 - (y^2)^2$, thus recognizing it as a difference of squares that can be factored as $(x^2 - y^2)(x^2 + y^2)$, or see $2x^2 + 8x$ as $(2x)(x) + 2x(4)$, thus recognizing it as a polynomial whose terms are products of monomials and the polynomial can be factored as $2x(x+4)$. | Reduce overall emphasis in earlier algebra-focused courses. | 1.9, 4.1, 4.2, 4.3, 4.4, 4.11, 4.12 | 20-1, 20-2, 20-3, 26-1, 26-2, 27-1, 27-2 |
| | A1: A.SSE.B.3 Conceptual, Procedural | Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression. | | | |
| | A1: A.SSE.B.3a Conceptual, Procedural | Factor a quadratic expression to reveal the zeros of the function it defines. | | | |
| 8.EE.A.2 | A1: A.SSE.B.3b Conceptual, Procedural | Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines. | Reduce the number of repetitious practice problems that would normally be assigned to students for this topic and emphasize the value of the form of the expression over fluency with the specific process of completing the square. Connect to students' work on A-REI.B.4a. | 4.11, 4.12, 4.16, 4.17, 4.21, 4.23 | SpringBoard Alg 1 contains no lesson directly aligned to this standard. |
| | A1: A.SSE.B.3c Procedural | Use the properties of exponents to transform expressions for exponential functions emphasizing integer exponents. For example, the growth of bacteria can be modeled by either $f(t) = 3^{(t+2)}$ or $g(t) = 9(3^t)$ because the expression $3^{(t+2)}$ can be rewritten as $(3^t)(3^2) = 9(3^t)$. | | | |
| 8.EE.A.1 | A1: A.APR.A.1 Conceptual, Procedural | Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials. | Less emphasis on adding/subtracting and more prioritize multiplying. Combine lessons with A- SSE 2 to address key concepts and reduce the amount of time spent on this standard. | 1.6, 1.7 (R), 1.8, 1.9, 4.1, 4.2, 4.3 | 24-1, 24-2, 24-3, 25-1, 25-3, 25-3 |
| | A1: A.APR.B.3 Conceptual, Procedural | Identify zeros of quadratic functions and use the zeros to sketch a graph of the function defined by the polynomial. | Eliminate content to save time. | 4.9 | 31-2, 31-3 |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--|---|--|--|---------------------------------|--|
| 8.EE.A.2, 8.EE.B.5, 8.EE.B.6, 8.F.B.4 | A1: A.CED.A.1 Conceptual, Procedural Application | Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear, quadratic, and exponential functions. | | | |
| | A1: A.CED.A.2 Conceptual, Procedural | Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales. | | | |
| | A1: A.CED.A.3 Conceptual, Application | Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods. | | | |
| 8.EE.C.7a-b | A1: A.CED.A.4 Procedural | Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law V = IR to highlight resistance R. | Reduce the number of repetitious practice problems that would normally be assigned to students for this topic. | | |
| 8.EE.C.7a-b | A1: A.REI.A.1 Conceptual | Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method. | Lessen the normal emphasis on problem types related to explaining each step and elevate the importance of constructing viable arguments. | 1.12, 1.13 | 2-1, 2-2, 2-3, 2-4 |
| 8.EE.C.7a-b | A1: A.REI.B.3 Procedural | Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. | Reduce the number of repetitious practice problems that would normally be assigned to students for this topic. | 1.12, 1.13, 1.14, 1.19, 1.25 | 2-1, 2-2, 2-3, 2-4, 3-1, 3-2, 3-3, 16-1, 16-2, |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--------------------------|---|---|---|---|---------------------------------------|
| 8.EE.A.2 | A1: A.REI.B.4 Procedural | Solve quadratic equations in one variable. | Reduce the normal emphasis. | 4.24 | 31-1, 32-1, 32-2, 32-3, 32-4, 33-2 |
| | A1: A.REI.B.4a Procedural | Use the method of completing the square to transform any quadratic equation in x into an equation of the form $(x - p)^2 = q$ that has the same solutions. Derive the quadratic formula from this form. | Lessen the normal emphasis on deriving the quadratic formula and reduce the number of repetitious practice problems that would normally be assigned to students for this topic. | 4.13, 4.14 | 32-1, 32-2, 32-3, 32-4 |
| | A1: A.REI.B.4b Conceptual, Procedural | Solve quadratic equations by inspection (e.g., for $x^2 = 49$), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as "no real solution." | Lessen the emphasis on completing the square and emphasize solving by inspection, taking square roots, quadratic formula, and factoring; recognize when quadratic formula gives non-real solutions but reduce emphasis on this case. | 1.17, 4.5, 4.6, 4.7, 4.13, 4.14, 4.15 | 31-1 |
| | • A1: A.REI.C.5 Conceptual | Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. | Eliminate content to save time | 1.23 | 17-3, 17-4, 17-5 |
| | • A1: A.REI.C.6 Procedural | Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables. | | | |
| | A1: A.REI.D.10 Conceptual | Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line). | | | |
| 8.EE.C.8a-c | A1: A.REI.D.11 Conceptual. Procedural | Explain why the x-coordinates of the points where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solutions of the equation $f(x) = g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions. | | | |
| | A1: A.REI.D.12 Procedural | Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes. | Emphasize problems that ground the mathematics in real world contexts. | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--------------------------|--|--|--|--------------------|------------------|
| 8.F.A.1 | A1: F.IF.A.1 Conceptual | Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If f is a function and x is an element of its domain, then $f(x)$ denotes the output of f corresponding to the input x. The graph of f is the graph of the equation $y = f(x)$. | | | |
| | A1: F.IF.A.2 Conceptual, Procedural | Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context. | | | |
| | A1: F.I.F.A.3 Conceptual | Recognize that sequences are functions whose domain is a subset of the integers. Relate arithmetic sequences to linear functions and geometric sequences to exponential functions. | Reduce the number of repetitious practice problems that would normally be assigned to students for this topic. | 3.1, 3.3, 3.5, 3.9 | 11-3, 21.1, 21.2 |
| 8.F.B.5 | A1: F.IF.B.4 Conceptual | For linear, piecewise linear (to include absolute value), quadratic, and exponential functions that model a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; and end behavior. | | | |
| | A1: F.IF.B.5 Conceptual | Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. For example, if the function $h(n)$ gives the number of person-hours it takes to assemble n engines in a factory, then the positive integers would be an appropriate domain for the function.* | | | |
| 8.F.B.4 | A1: F.IF.B.6 Conceptual, Procedural | Calculate and interpret the average rate of change of a linear, quadratic, piecewise linear (to include absolute value), and exponential function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph. | | | |
| | A1: F.IF.C.7 Conceptual, Procedural | Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases. | | | |
| | A1: F.IF.C.7a Conceptual, Procedural | Graph linear and quadratic functions and show intercepts, maxima, and minima. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--------------------------|--|--|---|--|--|
| | A1: F.IF.C.7b Procedural | Graph piecewise linear (to include absolute value) and exponential functions. | Eliminate step functions; emphasize square root and cube root. | 3.15, 3.16, 3.17, 3.18, 3.19, 3.20, 3.21, 3.23, 3.24 (E), 4.19, 4.20 | 14-3, 34-3 |
| | A1: F.IF.C.8 Conceptual, Procedural | Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function. | Reduce the number of repetitious practice problems related to | see alignment for A1: F-IF.C.8a | 32-1, 32-2, 32-3, 32-4 ,32-5 |
| | A1: F.IF.C.8a Conceptual, Procedural | Use the process of factoring and completing the square in a quadratic function to show zeros, extreme values, and symmetry of the graph, and interpret these in terms of a context. | factoring trinomials over the integers, and emphasize using the factored form to draw conclusions. Connect to HS.A-SSE.B.3b. | 4.9, 4.15, 4.16, 4.17, 4.21, 4.23, 5.4 | See alignment for F.IF.C.8 |
| 8.F.A.2 | A1: F.IF.C.9 Conceptual, Procedural | Compare properties of two functions (linear, quadratic, piecewise linear [to include absolute value] each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a graph of one quadratic function and an algebraic expression for another, determine which has the larger maximum. | Reduce the number of repetitious practice problems that would normally be assigned to students for this topic. | | |
| | A1: F.BF.A.1 Conceptual, Procedural | Write a linear, quadratic, or exponential function that describes a relationship between two quantities. | Reduce the normal emphasis | See alignment for A1: F-BF.A.1a | 10-1, 10-2, 29-1, 33-1, 34-1, 34-2, |
| | A1: F.BF.A.1a Conceptual, Procedural | Determine an explicit expression, a recursive process, or steps for calculation from a context. | Combine with F-BF.A.2, F-LE.A.2 and F-IF.A.3 to address key concepts and reduce the amount of time spent on this standard. | 3.5, 3.6, 3.7, 3.14, 3.21, 3.22, 3.23, 4.16, 4.23, 5.1, 5.2, 5.3, 5.4, 5.5, 5.6 | 10-1, 10-2, 34-2 |
| | • A1: F.BF.B.3 Conceptual | Identify the effect on the graph of replacing $f(x)$ by $f(x)+k,kf(x),f(kx)$, and $f(x + k)$ for specific values of k (both positive and negative). Without technology, find the value of k given the graphs of linear and quadratic functions. With technology, experiment with cases and illustrate an explanation of the effects on the graph that include cases where (x) is a linear, quadratic, piecewise linear (to include absolute value), or exponential function. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|-----------------------------------|---|---|--|----------------------|---------------------------|
| 8.EE.B.5, 8.EE.B.6, | A1: F.LE.A.1 Conceptual | Distinguish between situations that can be modeled with linear functions and with exponential functions. | | | |
| 8.F.A.3, 8.F.B.4 | A1: F.LE.A.1a Conceptual | Prove that linear functions grow by equal differences over equal intervals, and that exponential functions grow by equal factors over equal intervals. | | | |
| 8.F.A.3 | A1: F.LE.A.1b Conceptual | Recognize situations in which one quantity changes at a constant rate per unit interval relative to another. | | | |
| 0.F.A.5 | A1: F.LE.A.1c Conceptual | Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another. | | | |
| 8.EE.B.5, 8.EE.B.6, 8.F.B.4 | A1: F.LE.A.2 Conceptual, Procedural | Construct linear and exponential functions, including arithmetic and geometric sequences, given a graph, a description of a relationship, or two input-output pairs (include reading these from a table). | | | |
| | A1: F.LE.A.3 Conceptual | Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function. | Combine with F-LE.A.1b and F-LE.A.1c to address key concepts and reduce the amount of time spent on this standard. | 3.5, 3.6, 3.14, 3.21 | 22-3, 34-2, 34-3, 35-1 |
| | A1: F.LE.B.5 Conceptual | Interpret the parameters in a linear or exponential function in terms of a context. | | | |
| | • A1: S.ID.A.2 Conceptual, Procedural | Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets. | | | |
| | • A1: S.ID.A.3 Conceptual | Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers). | | | |
| 8.SP.A.4 | A1: S.ID.B.5 Conceptual, Procedural | Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations and trends in the data. | | | |



| Prerequisite Standard | Grade-Level Standard | Standard Language | Instructional Time | Eureka Math | SpringBoard |
|--------------------------|--|--|----------------------------|--------------------|-------------|
| | A1: S.ID.B.6 Conceptual, Procedural | Represent data on two quantitative variables on a scatter plot, and describe how the variables are related. | | | |
| 8.SP.A.1, | A1: S.ID.B.6a Conceptual, Procedural, Application | Fit a function to the data; use functions fitted to data to solve problems in the context of the data. Use given functions or choose a function suggested by the context. Emphasize linear and quadratic models. | | | |
| 8.SP.A.2 | A1: S.ID.B.6b Conceptual, Procedural | Informally assess the fit of a function by plotting and analyzing residuals. | | | |
| | A1: S.ID.B.6c Procedural | Fit a linear function for a scatter plot that suggests a linear association. | | | |
| 8.SP.A.3 | A1: S.ID.C.7 Conceptual | Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data. | | | |
| | A1: S.ID.C.8 Conceptual, Procedural | Compute (using technology) and interpret the correlation coefficient of a linear fit | Reduce the normal emphasis | 2.19, 2.20, 5.7 | 38-1, 38-2, |
| | A1: S.ID.C.9 Conceptual | Distinguish between correlation and causation. | | | |



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